## SURDS

| Keywords: | Rational / Irrational / Root / Surd / Expand / Rationalise |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Definition / Description: | Rational - A number that can be expressed as either an integer, a terminating decimal or a fraction | Irrational - A <br> number that cannot be expressed as either an integer, a terminating decimal or a fraction | Root - A root is a quantity that when multiplied by itself a certain number of times equals a given quantity | Surd - An expression that includes a square root | Expand - To multiply out a set of brackets. | Rationalise - To eliminate an irrational number from the denominator of a fraction. |
| Knowledge points: | Simplify Surds - Simplify by factoring out a square number | Multiply and Divide Surds $\begin{gathered} \sqrt{a b}=\sqrt{a} \times \sqrt{b} \\ \sqrt{a \div b}=\sqrt{a} \div \sqrt{b} \end{gathered}$ | Add and Subtract Surds - When adding and subtracting surds the root must be the same number. | Expand Brackets with Surds Multiply each term inside the bracket by the term outside the bracket. | Rationalise the Denominator 1 Create an equivalent fraction where the denominator is rational | Rationalise the Denominator 2 Use a difference o two squares to rationalise |
| Knowledge point examples: | $\begin{aligned} & \sqrt{75}=\sqrt{25 \times 3} \\ & =\sqrt{25} \times \sqrt{3} \\ & =5 \times \sqrt{3} \\ & =5 \sqrt{3} \end{aligned}$ $\begin{aligned} & \sqrt{18}=\sqrt{9 \times 2} \\ & =\sqrt{9} \times \sqrt{2} \\ & =3 \times \sqrt{2} \\ & =3 \sqrt{2} \end{aligned}$ | $\begin{aligned} & \sqrt{6} \times \sqrt{7}= \\ & \sqrt{6 \times 7}= \\ & \sqrt{42} \\ & \sqrt{50} \div \sqrt{10}= \\ & \sqrt{50 \div 10}= \\ & \sqrt{5} \\ & 4 \sqrt{6} \times 2 \sqrt{5} \\ & =4 \times 2 \times \sqrt{6} \times \sqrt{5} \\ & =8 \sqrt{30} \end{aligned}$ | $5 \sqrt{2}+2 \sqrt{2}=7 \sqrt{2}$ $\begin{aligned} & \sqrt{75}-\sqrt{27} \\ & =5 \sqrt{3}-3 \sqrt{3} \\ & =2 \sqrt{3} \end{aligned}$ $\begin{aligned} & \sqrt{98}-\sqrt{50} \\ & =7 \sqrt{2}-5 \sqrt{2} \\ & =2 \sqrt{2} \end{aligned}$ | $\begin{aligned} & \sqrt{3}(\sqrt{7}+5) \\ & =\sqrt{21}+5 \sqrt{3} \end{aligned}$ $\begin{aligned} & =5+4 \sqrt{5}-2 \sqrt{5}-8 \\ & =2 \sqrt{5}-3 \end{aligned}$ | $\frac{2 \times \sqrt{3}}{\sqrt{3} \times \sqrt{3}}=\frac{2 \sqrt{3}}{3}$ $\frac{3}{2 \sqrt{5}}=\frac{3 \sqrt{5}}{2 \times 5}=\frac{3 \sqrt{5}}{10}$ | $\begin{gathered} \frac{2}{4+\sqrt{2}}= \\ \frac{2(4-\sqrt{2})}{4+\sqrt{2})(4-\sqrt{2})}= \\ \frac{8-2 \sqrt{2}}{4^{2}-(\sqrt{2})^{2}}= \\ \frac{8-2 \sqrt{2}}{12} \end{gathered}$ |

## Linked Knowledge Maps

