

# **Toynbee Curriculum Knowledge Maps**

# **MATHS (Data and Probability)**

**Toynbee School**



# SIMPLE PROBABILITY

<b>Keywords:</b>	Trial, Event, Outcome, Random, Experimental probability, Relative frequency, Theoretical probability, Estimate, Independent			
<b>Definition / Description:</b>	Trial: a test or experiment Event: an occurrence or outcome Outcome: possible results of an experiment Random: Something that happens without bias Biased: having a tendency towards something away from the normal Mutually Exclusive: events that cannot happen at the same time Estimate: give an approximation of the actual value Independent: events that do not depend on each other			
<b>Knowledge points –</b>	<b>Experimental probability</b> (Relative frequency): a probability that is determined on the basis of a series of experiments	<b>Theoretical probability:</b> what is expected to happen based on the possible outcomes, assuming equalling likely events	<b>The OR rule:</b> In mutually exclusive events, to find the probability of one event OR another event happening we ADD the probabilities	<b>The AND rule:</b> In Independent events, to find the probability of one event AND another happening, we MUTLIPLY the probabilities
<b>Knowledge point examples:</b>	<p><b>Experimental Probability</b> is found by repeating an experiment and observing the outcomes.</p> $P(\text{event}) = \frac{\text{number of times event occurs}}{\text{total number of trials}}$ <p><b>Example:</b>            A coin is tossed 10 times:            A head is recorded 7 times and a tail 3 times.</p> $P(\text{head}) = \frac{7}{10}$ $P(\text{tail}) = \frac{3}{10}$	<p><b>Theoretical Probability</b> is what is expected to happen based on mathematics</p> $P(\text{event}) = \frac{\text{number of favorable outcomes}}{\text{total number of possible outcomes}}$ <p><b>Example:</b>            A coin is tossed.</p> $P(\text{head}) = \frac{1}{2}$ $P(\text{tail}) = \frac{1}{2}$	$P(A \text{ OR } B) = P(A) + P(B)$ <p>When two dice are rolled, the probability of getting a 3 OR a 4 =</p> $P(3 \text{ and } 4) = P(3) + P(4)$ $= \frac{1}{6} + \frac{1}{6}$ $= \frac{2}{6}$ $= \frac{1}{3}$	$P(A \text{ and } B) = P(A) \times P(B)$ <p>When two dice are rolled, the probability of getting a 3 AND a 4 =</p> $P(3 \text{ and } 4) = P(3) \times P(4)$ $= \frac{1}{6} \times \frac{1}{6}$ $= \frac{1}{36}$
<b>Linked Knowledge Maps:</b>	Further Probability Fractions Ratio			

# FURTHER PROBABILITY

**Keywords:** Event / Independent / Dependent / Conditional

**Definition / Description:**

**Event:** A particular result or set of results amongst the possibilities

**Independent:** events that have no impact on each other's results.

**Dependent:** events that have an impact on each other's results.

**Conditional:** the probability of an event (A), given that another (B) has already occurred

**Knowledge points:**

Tree diagrams Independent events: The outcome of the 1<sup>st</sup> event does not effect the probability of the 2<sup>nd</sup> event

Tree Diagrams Dependent events: The probability of the 2<sup>nd</sup> event is dependent on the outcome of the 1<sup>st</sup> event

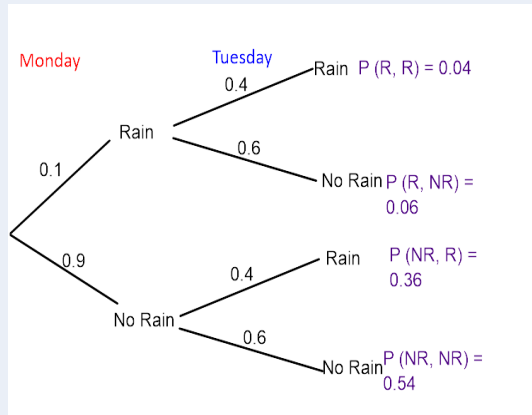
Conditional Probability: The probability of second event given the outcome of the first

**Knowledge point examples:**

The probability of it raining on Monday and Tuesday is shown in the tree diagram.

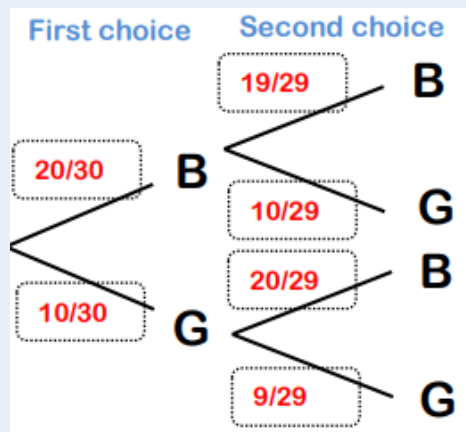
Find the probability it rains on both days:  $P(RR) = 0.1 \times 0.4 = 0.04$

Find the probability it rains on one day:  $P(NRR) + P(RNR) = 0.06 + 0.36 = 0.42$



There are 20 boys and 10 girls in a class. Two pupils are chosen at random. What is the probability that a girl and boy are chosen?

$$P(GB) + P(BG) = \left(\frac{10}{30} \times \frac{19}{29}\right) + \left(\frac{20}{30} \times \frac{10}{29}\right) = \frac{40}{87}$$



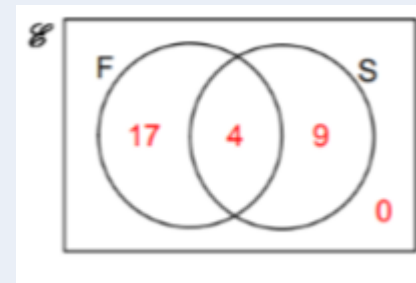
What is the probability of choosing a boy given they travel by car?

$$\frac{9}{13}$$

	Walk	Car	Total
Boys	16	9	25
Girls	18	4	22
Total	34	13	47

What is the probability that a student, given they study French, studies Spanish?

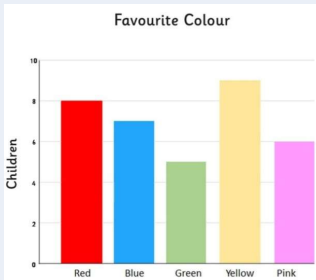


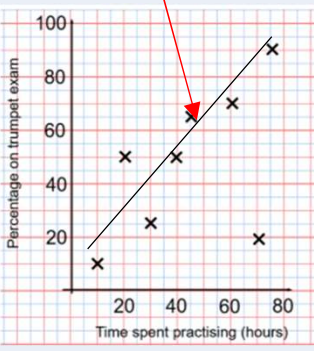
$$= \frac{17}{21}$$



**Linked Knowledge Maps:**

Basic Probability  
Fractions  
Ratio

# STATISTICS – UNGROUPED DATA

<b>Keywords:</b>	Data / Sample / Frequency Table / Correlation / Discrete Data / Continuous Data																					
<b>Definitions/ Descriptions</b>	<b>Data:</b> A collection of numbers or information	<b>Sample:</b> Contains all possible outcomes of an experiment	<b>Frequency Table:</b> An arrangement of data in columns	<b>Correlation:</b> The connection between two variables	<b>Discrete Data:</b> Separate or distinct items of data	<b>Continuous Data:</b> Data that is arranged into groups with no gaps																
<b>Knowledge points:</b>	<b>Bar Chart</b> - uses bars of equal lengths to represent statistics	<b>Pie Chart</b> – uses different sized sectors of a circle to represent data	<b>Pictogram</b> – a chart that uses pictures or symbols to represent data	<b>Scatter Graph</b> – compares two variables by plotting one value against the other	<b>Two Way Table</b> – used when handling data to illustrate two variables																	
<b>Knowledge point examples:</b>	<b>Bar Chart:</b> 	<b>Pie Chart</b> 	<b>Pictograms:</b> <ul style="list-style-type: none"> <li>Pop: 4 CD icons</li> <li>Rock: 2 CD icons</li> <li>Blues: 3 CD icons and 1 quarter CD icon</li> <li>Jazz: 3 CD icons and 1 quarter CD icon</li> <li>Classical: 2 CD icons and 1 quarter CD icon</li> </ul> <p>Key:  = 4 CDs</p>	<b>Scatter Graphs</b>  <p>(Positive correlation)</p>	<b>Two Way Table</b> <table border="1" data-bbox="1769 790 2206 949"> <thead> <tr> <th></th> <th>Boys</th> <th>Girls</th> <th>Totals</th> </tr> </thead> <tbody> <tr> <td>Running</td> <td>6</td> <td>9</td> <td>15</td> </tr> <tr> <td>Swimming</td> <td>13</td> <td>12</td> <td>25</td> </tr> <tr> <td>Totals</td> <td>19</td> <td>21</td> <td>40</td> </tr> </tbody> </table> <p>Dora did a survey of her class whether they prefer running or swimming. She recorded the results in a two-way table</p>			Boys	Girls	Totals	Running	6	9	15	Swimming	13	12	25	Totals	19	21	40
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<b>Linked Knowledge Maps:</b>	Statistics – grouped Data																					

# Statistics – Grouped Data

**Keywords:** Histogram / Frequency Density / Class Interval / Distribution / Cumulative / Frequency / Polygon / Median / Interquartile range / Box Plot / Estimated Mean

**Definition / Description:**

- Cumulative Frequency** diagram represents a running total of frequencies as a graph
- Box Plot** visually shows the distribution of data by identifying five points in a data set
- Interquartile range** measures the spread of data between the upper and lower quartiles. A small interquartile range shows consistent data
- Histogram** is a graphical representation of data points organised into ranges
- Frequency density** is the frequency per unit for the data in each class. It is used to plot histograms
- Class interval** is the numerical width of any class in a particular distribution, defined as the difference between the upper class limit and the lower class limit
- Estimated Mean** is the average using midpoints of grouped data.

**Knowledge points:**

- Cumulative Frequency:**
  - Calculate the running total
  - Plot at the Upper boundary of class
  - Join with a smooth curve
- Box Plot:**

5 points from data needed:

  - Minimum value
  - Lower quartile
  - Median
  - Upper quartile
  - Maximum value
- Interquartile range:**

Subtract Lower quartile from Upper quartile
- Histogram:**
  - Find class width of each category
  - Divide frequency by class width to find Frequency Density
- Estimated Mean:**
  - Find midpoint of data range
  - Multiply each frequency by this midpoint to find a breakdown of total
  - Add up breakdown of totals to find final total
  - Divide final total by total frequency

**Knowledge point examples:**

A cyclist records the number of miles he travels each week

Weeks	Number of miles (frequency)	Cumulative Frequency
1	17	17
2	19	36
3	42	78
4	38	116
5	14	130

Here is some information about the amount of cola contained in a sample of bottles from machine A.

Minimum	Lower quartile	Median	Upper quartile	Maximum
496 ml	502 ml	508 ml	510 ml	514 ml

Draw a box plot to represent this information.

Time taken (t seconds)	Class Width	Frequency	Frequency Density
10 < t < 30	20	5	0.25
30 < t < 40	10	8	0.8
40 < t < 50	10	16	1.6
50 < t < 70	20	24	1.2

Speed (mph)	Frequency (f)	Midpoint (m)	f x m
20 ≤ s < 25	4	22.5	90
25 ≤ s < 30	10	27.5	275
30 ≤ s < 35	12	32.5	390
35 ≤ s < 40	15	37.5	562.5
40 ≤ s < 45	9	42.5	382.5
<b>Total</b>	<b>50</b>		<b>1700</b>

Mean = Total sum ÷ total Frequency  
 = 1700 ÷ 50  
 = 34 mph

**Linked Knowledge Maps:** Statistics – ungrouped data Averages